

Electromagnetic ion cyclotron (EMIC) waves in warm plasmas

Lunjin Chen, Richard Thorne, and
Jacob Bortnik

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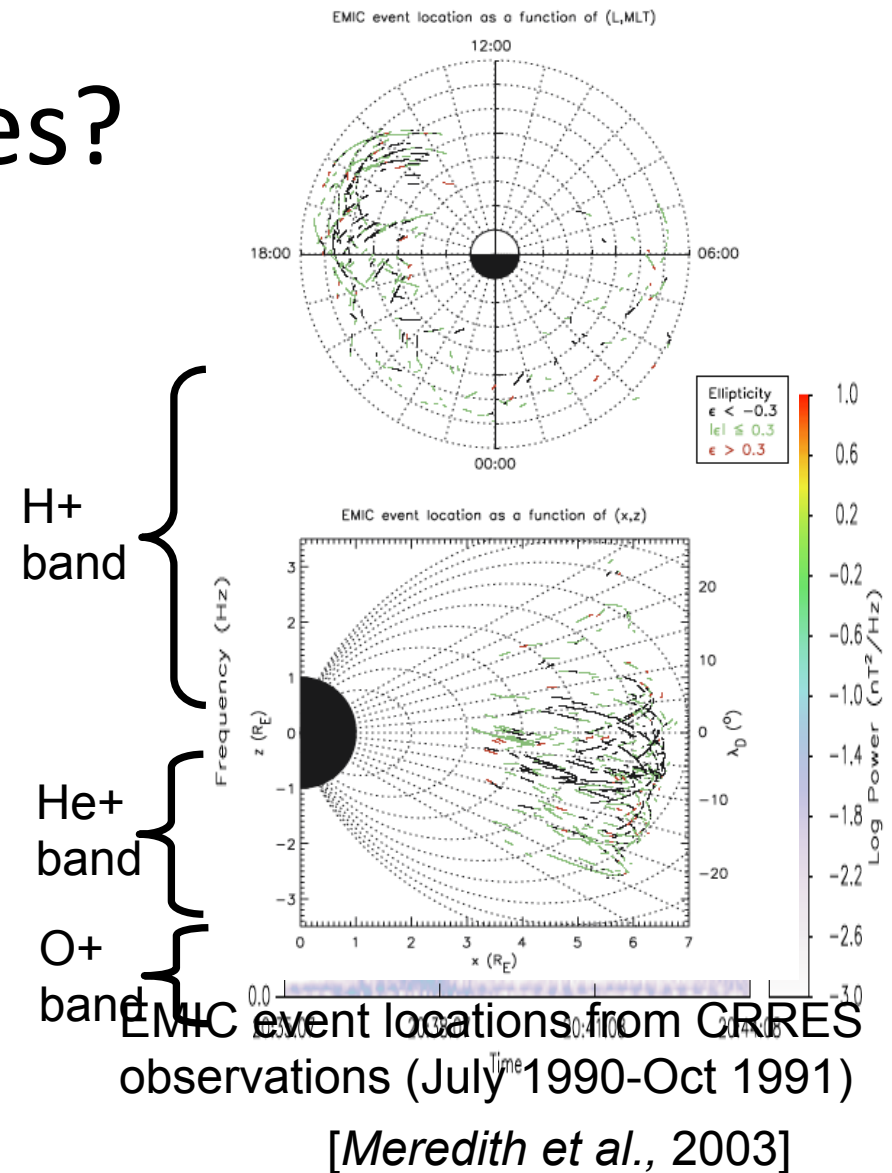
What are EMIC waves?

- Left-handed polarization
 - Below ion gyro-frequency (\sim Hz)
 - Multiple-band structure
 - Stronger emission in He⁺ band
- [Meredith et al., 2003, Fraser et al., 2010]

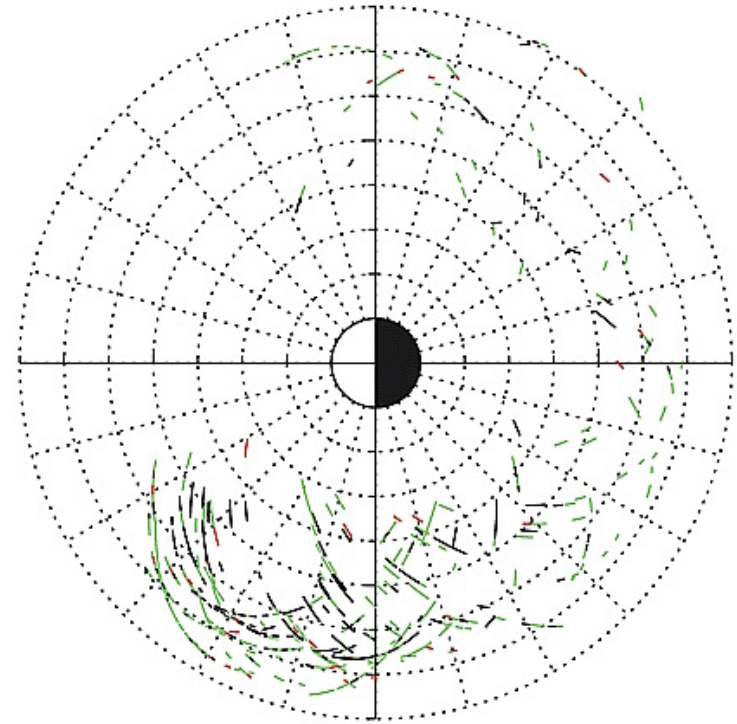
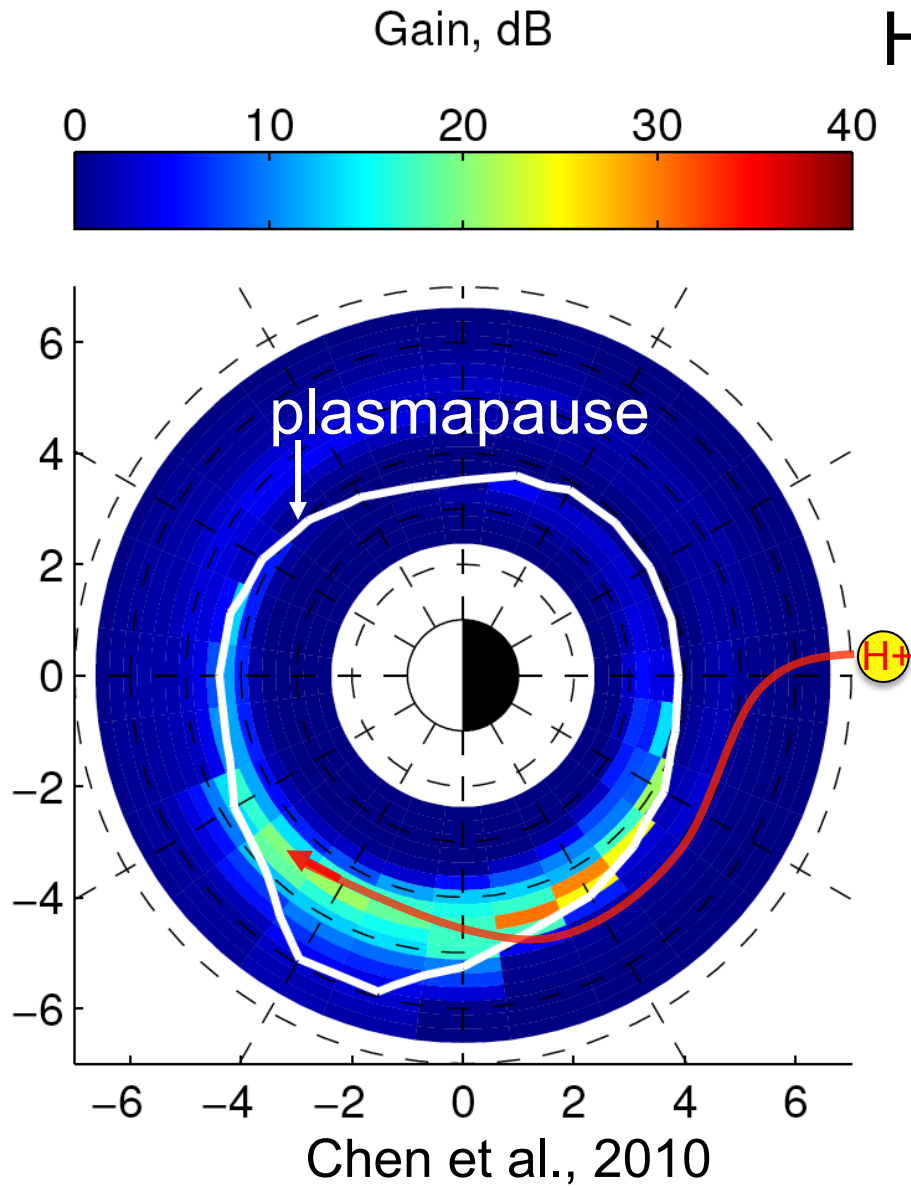
Where and when?

- Source region within $\pm 11^\circ$ of the equator
- 82% observed in 1300-2000 MLT, $L > 3$
- Occurrence rate 5 times higher during storm times than quiet time

[Loto'aniu et al., 2005, Fraser and Nguyen, 2001, Erlandson and Ukhorskiy, 2001]



How to generate EMIC waves?

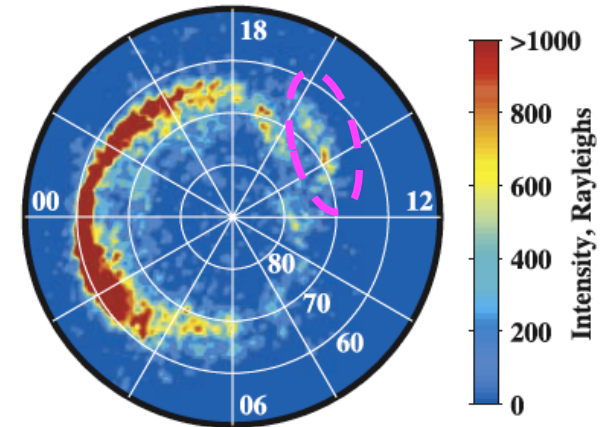


EMIC waves are generated in the duskside plume and nightside plasmopause, where ring current anisotropic H⁺ ($T_p > T_z$) overlaps high plasma density.

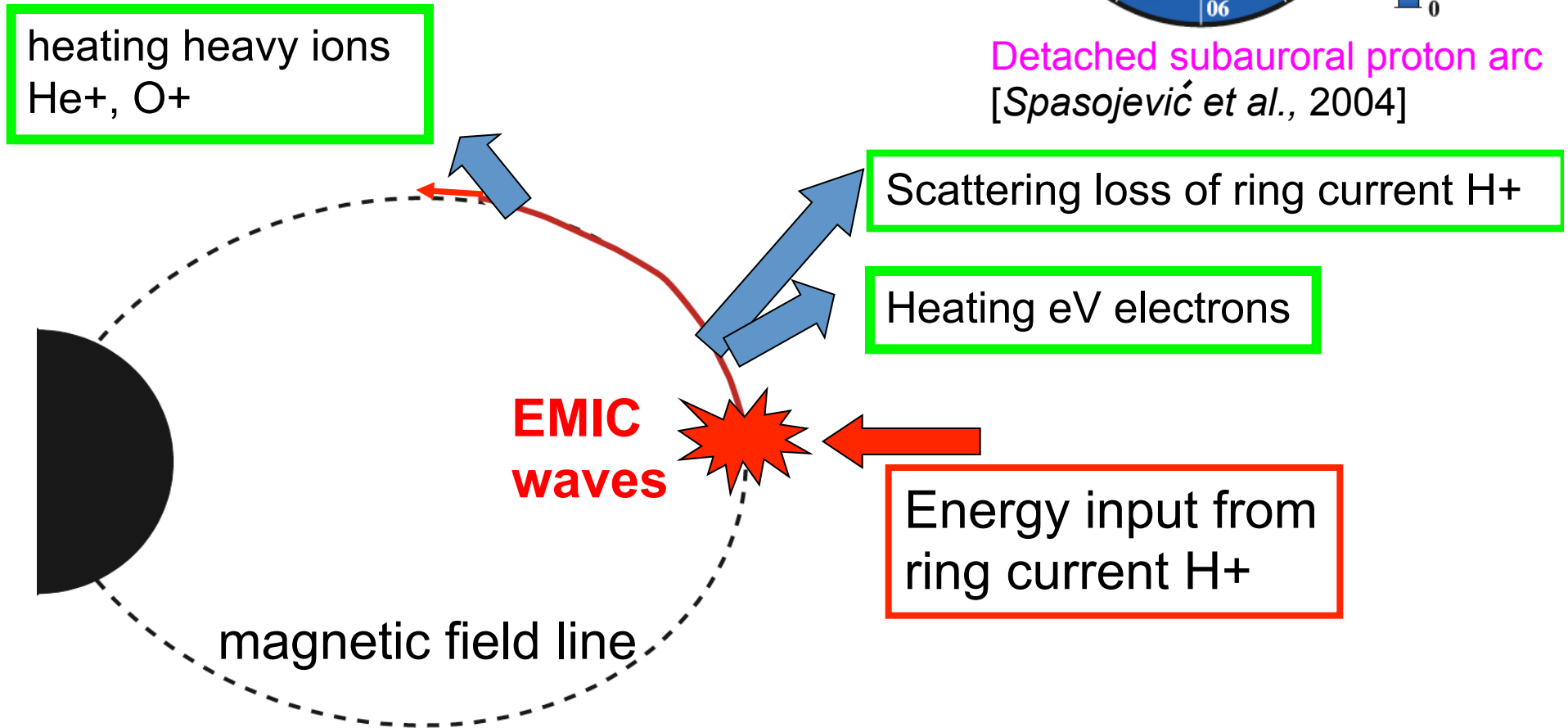
EMIC waves are agents for energy and momentum exchange between different groups of particles.

[*Thorne et al., 2006 Review*]

FUV SI12 Image 18 Jun 2001 15:50 UT



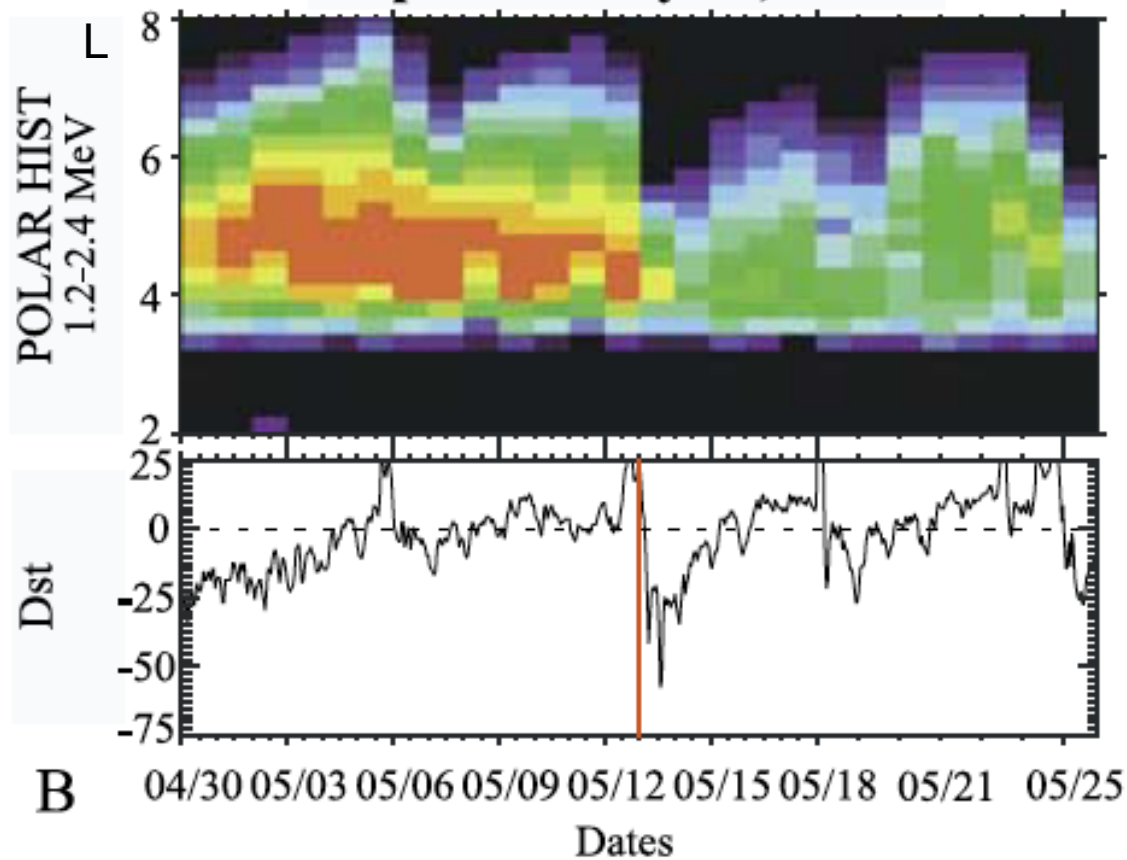
Detached subauroral proton arc
[*Spasojević et al., 2004*]



EMIC waves are also proposed to cause dramatic loss of MeV electrons over a time scale of hours during main phase of geomagnetic storms. [*Thorne and Kennel 1971*]

Relativistic electron flux dropout during main phase

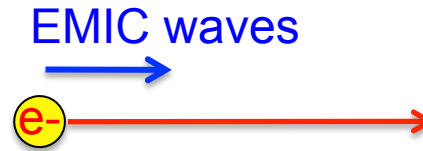
April 30-May 25, 1999



[*Reeves et al., 2003*]

Condition for Resonant Interaction between EMIC waves and electrons

$$\omega - kv_{e\parallel} = \Omega_e$$



$$E_{min}^- = \left(\sqrt{\frac{m_{H+}}{m_e} \frac{1}{y^2 f^2} + 1} - 1 \right) E_0$$

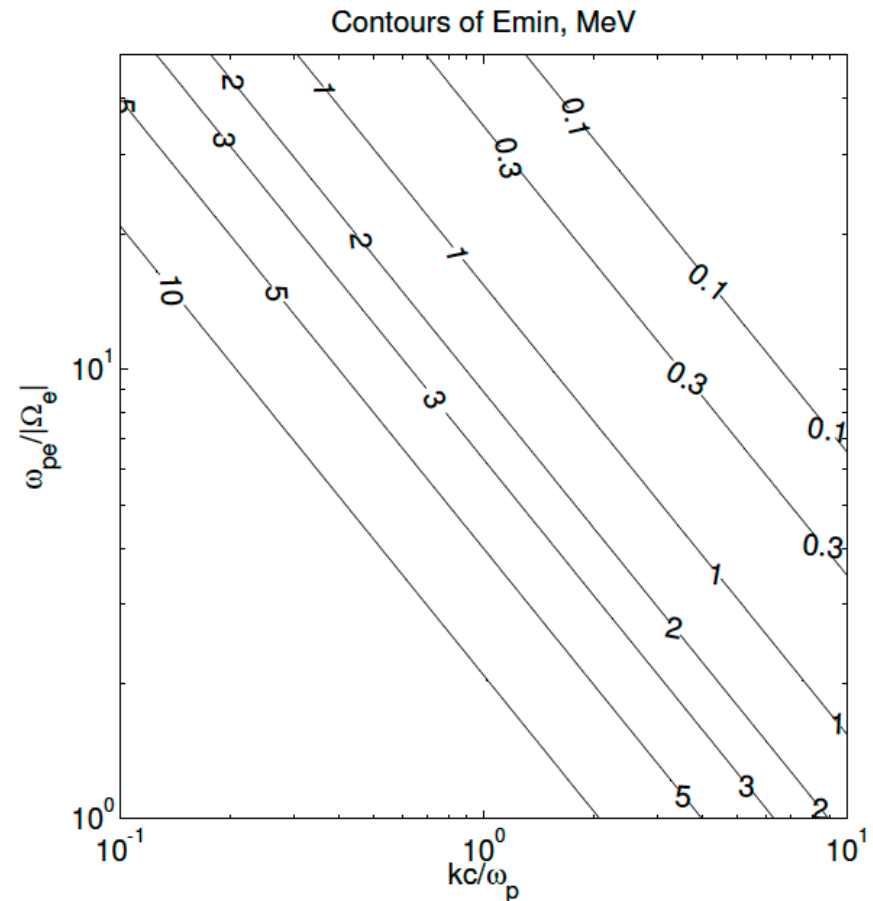
E_0 electron rest mass energy 511 keV

$y = kc/\omega_p$

$f = \omega_{pe}/|\Omega_e|$

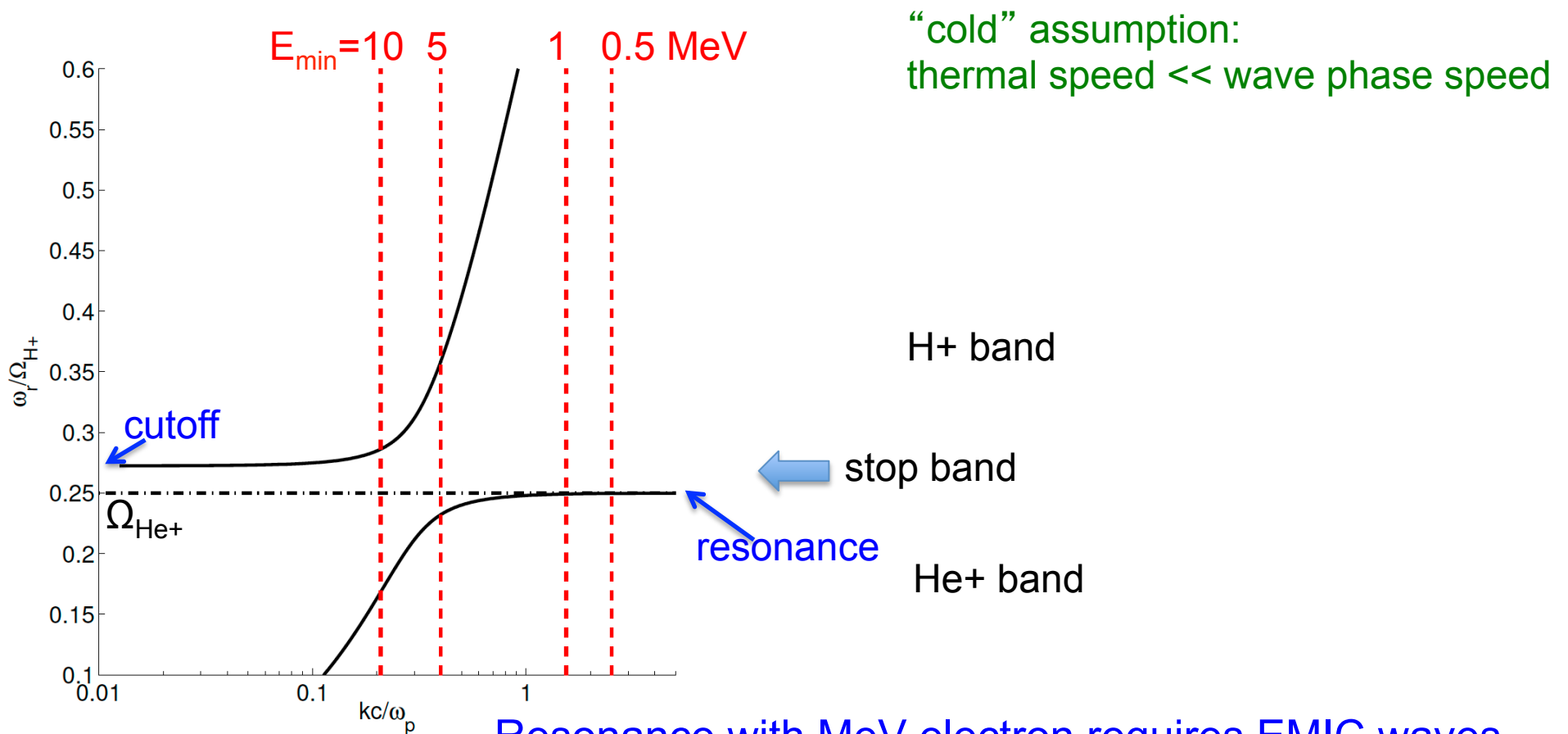
ω_p proton plasma frequency

$yf = 15.4$ for $E_{min} = 1$ MeV



Resonance with 1 MeV requires large wave number.

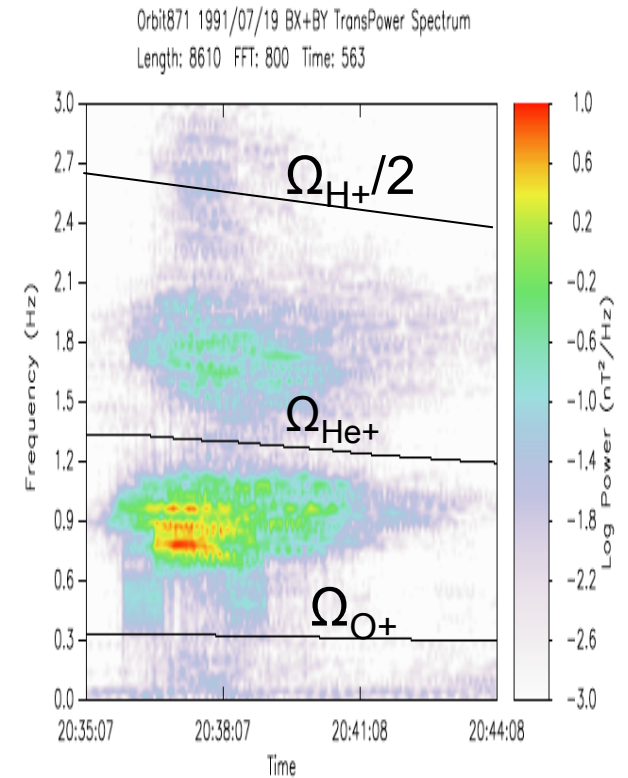
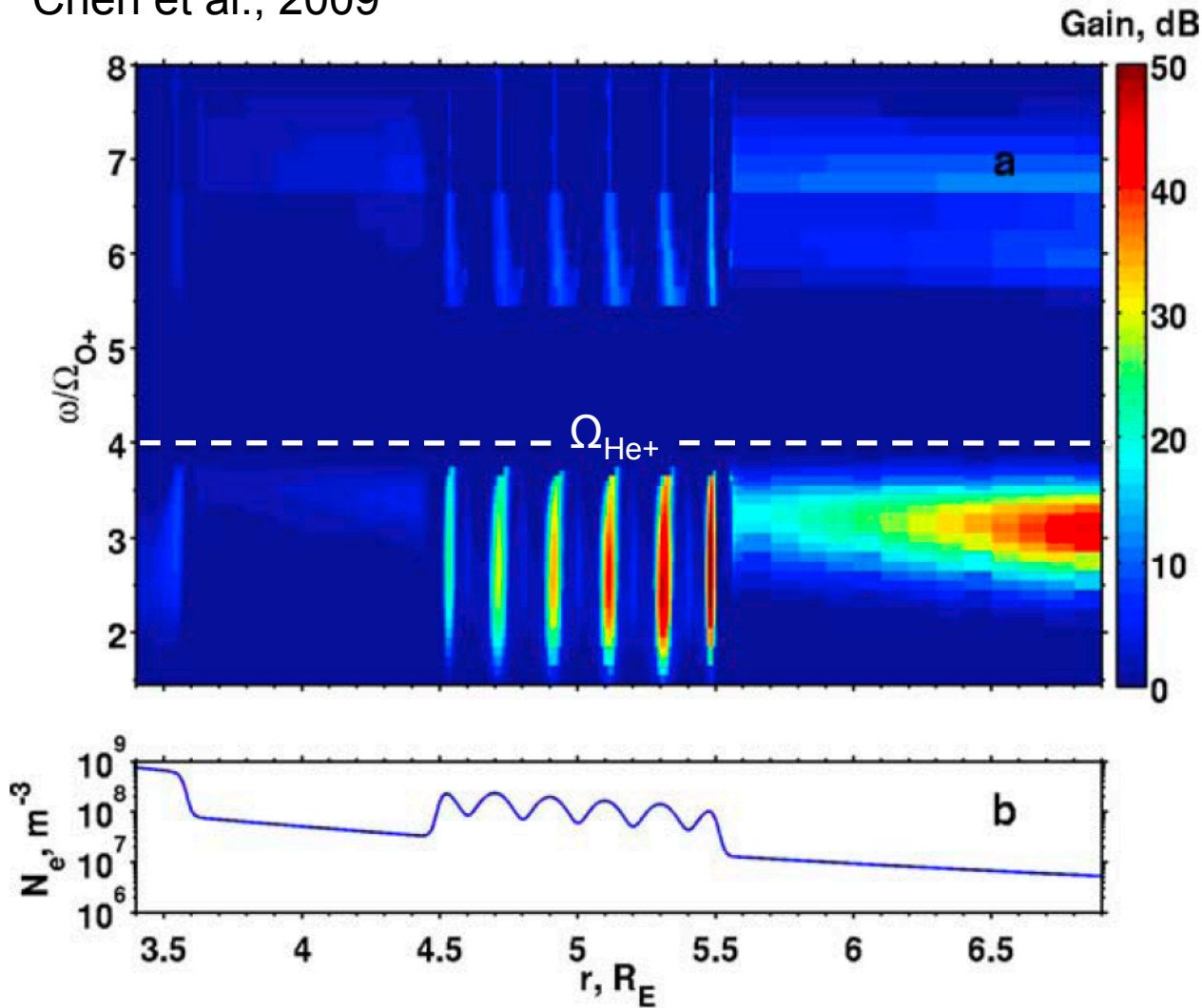
Dispersion Relation of EMIC waves in cold H⁺-He⁺ plasma



Resonance with MeV electron requires EMIC waves very close to Ω_{he^+} , from cold plasma theory

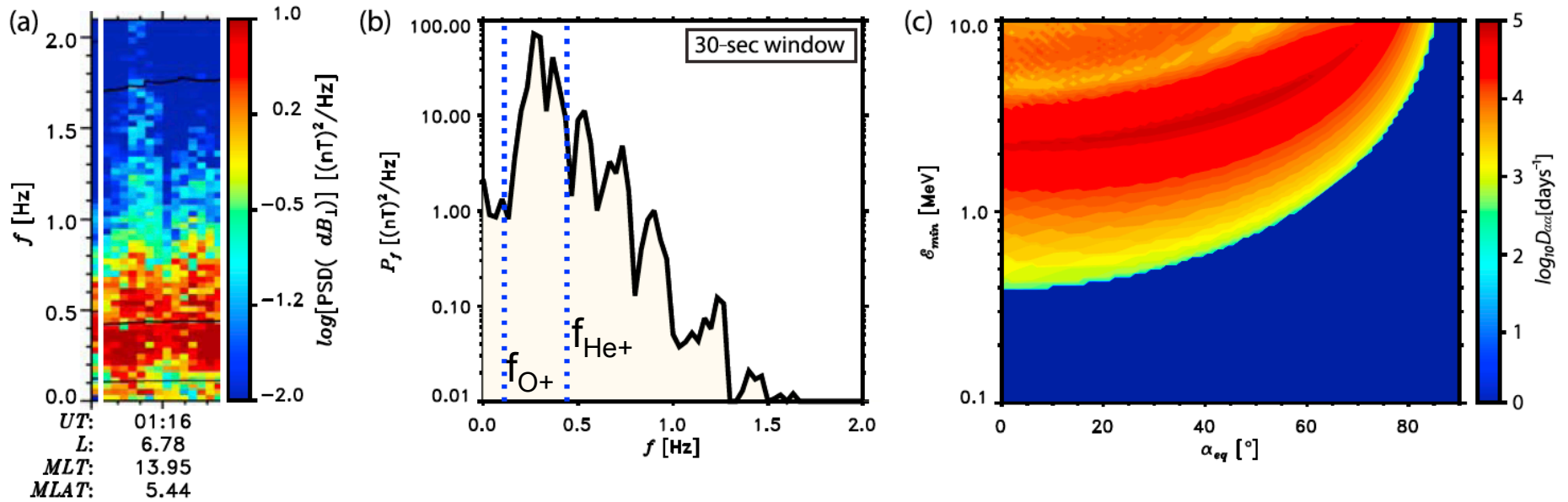
Simulation of EMIC wave spectrum

Chen et al., 2009



However, EMIC waves near Ω_{He^+} are generally suppressed, due to strong cyclotron damping due to thermal He⁺.

Large amplitude EMIC wave activity measured at AMPTE CCE during storm main phase [Ukhorskiy et al., 2010]



Wave power as a function of f

Electron scattering rate

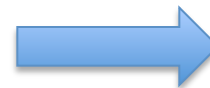
Cold plasma dispersion relation

How accurate?
Why no stop band?
Instability near Ω_{He^+} ?

Wave number

Electron resonant energy

Resonant condition



EMIC waves in warm H⁺-He⁺ plasma

Chen et al., 2011

$$\begin{aligned}
 y^2 = & \boxed{(x/f)^2 m_e/m_{H^+}} \quad \boxed{-x} \quad + \quad \boxed{(1 - \eta_{hh} - \eta_{he}) \frac{x}{1-x}} \quad + \quad \boxed{\frac{\eta_{he} x}{4x-1} \zeta_{he} Z(\zeta_{he})} \\
 & + \quad \boxed{\eta_{hh} \left[A_{hh} + \left(A_{hh} + \frac{x}{x-1} \right) \zeta_{hh} Z(\zeta_{hh}) \right]}, \quad (1)
 \end{aligned}$$

Anisotropic ring current H⁺ (hh)

$$x = \omega/\Omega_{H^+} = \omega_r/\Omega_{H^+} + i\omega_i/\Omega_{H^+}$$

$$y = kc/\omega_p$$

$$f = \omega_{pe}/|\Omega_e|$$

$$\omega_p = \sqrt{N_e e^2 / (\epsilon_0 m_{H^+})}$$

$$A_{hh} = \hat{T}_{hh\perp} / \hat{T}_{hh\parallel} - 1$$

Cold plasma limit

$$\lim_{|\zeta| \rightarrow \infty} \zeta Z(\zeta) = -1$$

$$\zeta = \frac{\omega - \Omega}{k v_{th\parallel}}$$

1) $v_{th} \ll v_{ph}$

2) $\omega \neq \Omega$

Z plasma dispersion function [Fried and Conte, 1961]

“Simplified” Dispersion Relation

$$D(x, y; f, \eta_{he}, T_{he}, \eta_{hh}, T_{hh\parallel}, A_{hh}) = 0$$

A complex equation

Complex wave frequency $x = x_r + i x_i$

Real wave number y

6 free parameters

Nominal case:

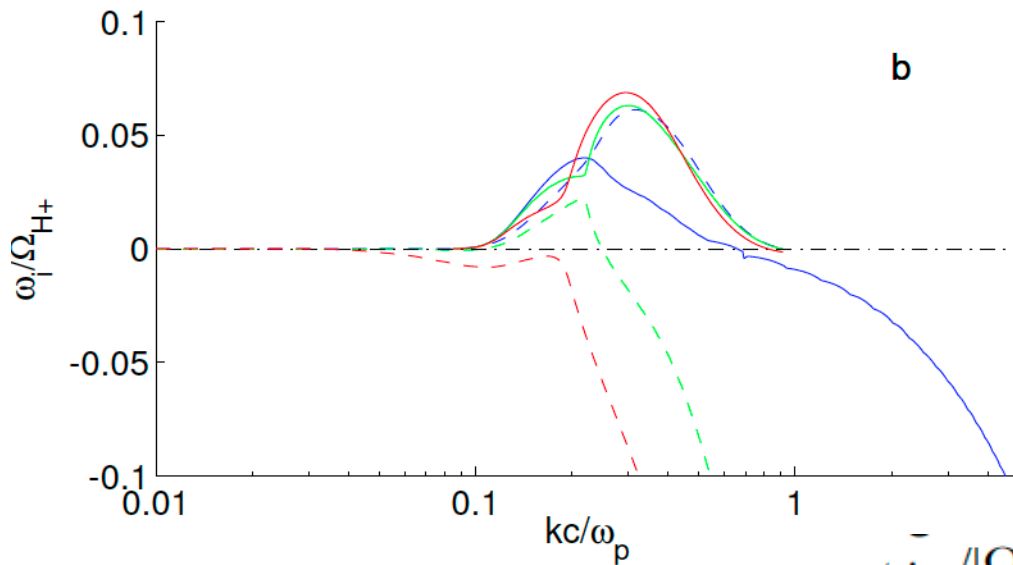
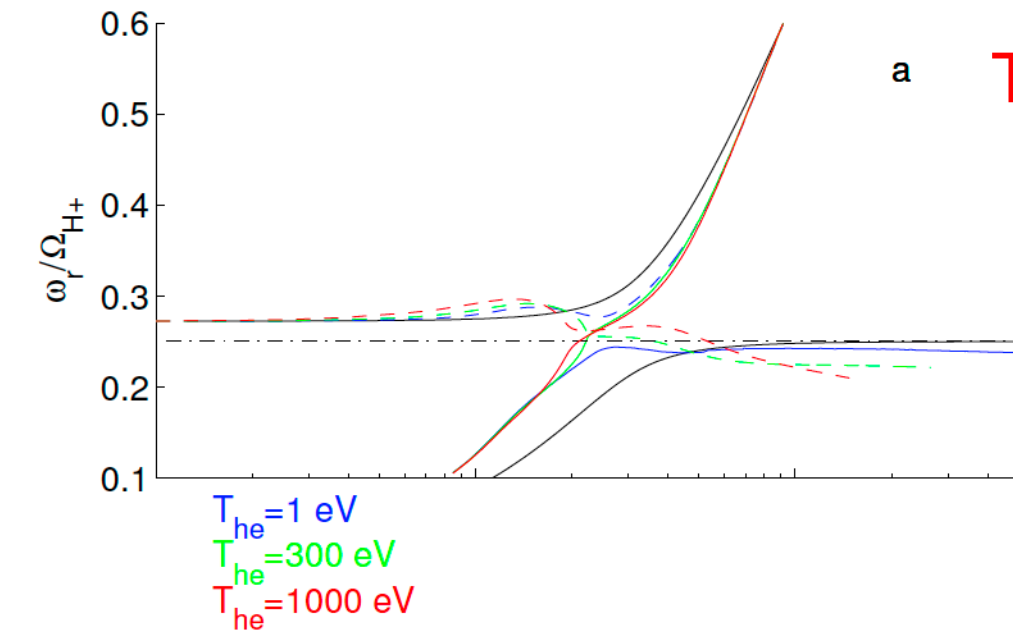
$$\bar{\omega}_{pe}/|\Omega_e| = 10$$

$$\eta_{he} = 3\%, T_{he} = 300 \text{ eV}$$

$$\eta_{hh} = 10\%, T_{hh\parallel} = 25 \text{ keV}, A_{hh} = 1.5$$

a The effect of He+ temperature

- 1) w-k not longer monotonic relation
- 2) Pronounced modification near Ω_{He^+}
- 3) Allowable solution at exact Ω_{He^+}
- 4) Two band structure and stop band disappear
- 5) Damping at high wave number ($y > 1$)



$$\bar{\omega}_{pe}/|\Omega_e| = 10$$

$$\eta_{he} = 3\%, T_{he} = 300 \text{ eV}$$

$$\eta_{hh} = 10\%, T_{hh\parallel} = 25 \text{ keV}, A_{hh} = 1.5$$

Green: nominal case

EMIC waves at Ω_{He^+}

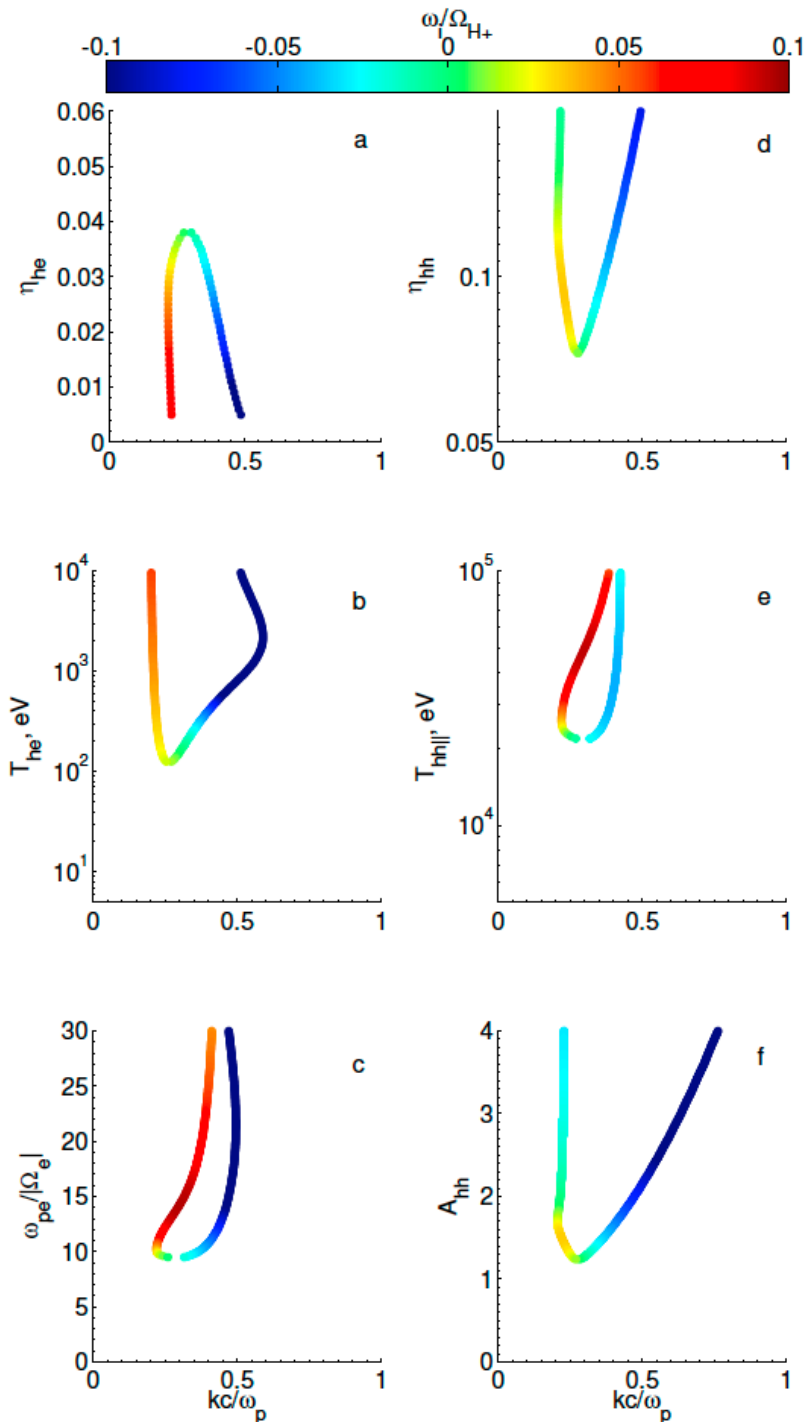
Solve for (x_i, y) with a fixed $x_r=1/4$ (i.e., $\omega=\Omega_{\text{He}^+}$) and varying one of the six parameters

➤ The presence and instability of waves exactly at Ω_{He^+} are due to the dominance of hot H+ growth over warm He+ damping, i.e., a less dense but sufficiently hot He+, a sufficiently dense, hot and anisotropic H+ together with a sufficiently dense cold plasma.

➤ Stop band must exist if any of these conditions fails.

➤ These waves can directly heat the thermal He+ ions.

➤ These waves, if excited, are not favorable to scatter 1 MeV because of limited wave number.



Resonance with 1 MeV electrons

Solve $D(x, y; f, \eta_{he}, T_{he}, \eta_{hh}, T_{hh||}, A_{hh}) = 0$

for x with a fixed $y=15.4/f$ and a huge set (7×10^5) of plasma conditions:
 $f = 5, 10, \dots, 30$; $\eta_{he} = 2\%, 4\%, \dots, 30\%$; $T_{he} = 1, 3, 5, 10, \dots, 3000, 5000$ eV
 $\eta_{hh} = 2\%, 4\%, \dots, 20\%$; $T_{hh} = 5, 10, 20, 30, \dots, 100$ keV; $A_{hh} = 0.5, 1, \dots, 3$.

and require that solutions of x must satisfy $x_r > 0.01$.

Table 1. Necessary (but Not Sufficient) Plasma Conditions That Are Unstable to L-Mode Waves Capable of Resonating With Relativistic Electrons of Energy Down to 1 MeV^a

A_{hh}	f	15	20	25	30
1		X	X	$\eta_{he} \geq 28\%, \eta_{hh} \geq 20\%, T_{he} \leq 1$	$\eta_{he} \geq 6\%, \eta_{hh} \geq 12\%, T_{he} \leq 10$
		X	X	X	$\eta_{he} \leq 8\%, \eta_{hh} \geq 10\%$
1.5		X	X	$\eta_{he} \geq 6\%, \eta_{hh} \geq 12\%, T_{he} \leq 10$	$\eta_{hh} \geq 8\%$
		X	$\eta_{he} \leq 4\%, \eta_{hh} \geq 18\%$	$\eta_{he} \leq 18\%, \eta_{hh} \geq 8\%$	$\eta_{he} \leq 26\%, \eta_{hh} \geq 6\%$
2.0		X	$\eta_{he} \geq 18\%, \eta_{hh} \geq 18\%, T_{he} \leq 3$	$\eta_{hh} \geq 10\%, T_{he} \leq 10$	$\eta_{hh} \geq 4\%$
		X	$\eta_{he} \leq 20\%, \eta_{hh} \geq 10\%$	$\eta_{hh} \geq 6\%$	$\eta_{hh} \geq 4\%$
2.5		X	$\eta_{he} \geq 8\%, \eta_{hh} \geq 14\%, T_{he} \leq 10$	$\eta_{hh} \geq 8\%$	$\eta_{hh} \geq 4\%$
		$\eta_{he} \leq 8\%, \eta_{hh} \geq 16\%$	$\eta_{hh} \geq 6\%$	$\eta_{hh} \geq 4\%$	$\eta_{hh} \geq 4\%$
3		X	$\eta_{he} \geq 4\%, \eta_{hh} \geq 12\%, T_{he} \leq 50$	$\eta_{hh} \geq 6\%$	$\eta_{hh} \geq 4\%$
		$\eta_{he} \leq 20\%, \eta_{hh} \geq 12\%$	$\eta_{hh} \geq 6\%$	$\eta_{hh} \geq 4\%$	Full

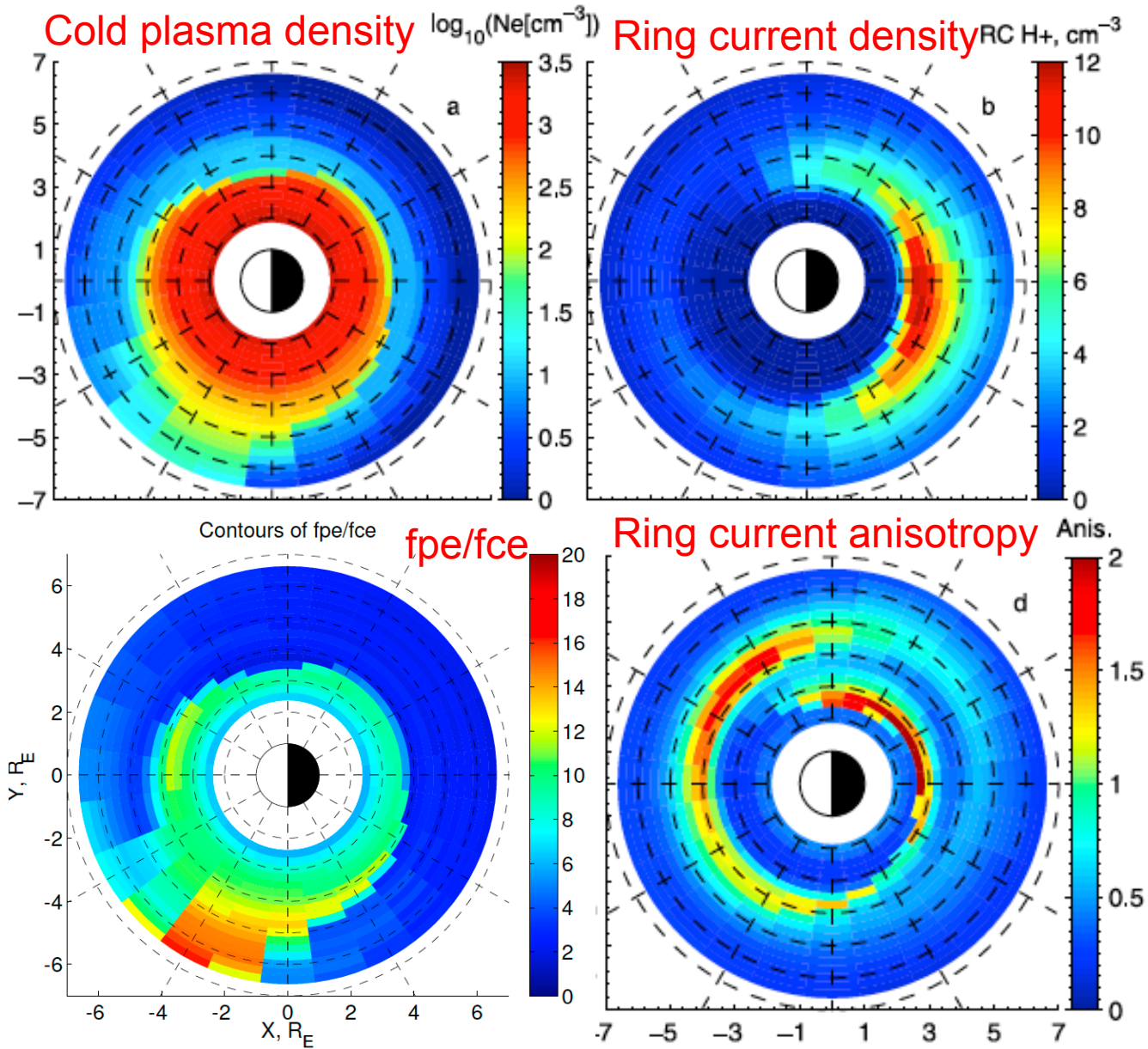
$x_r \leq 0.25$

$x_r > 0.25$

Most favorable plasma condition occurs only in the large f (≥ 15) and A_{hh} (≥ 1) regime.

For $x_r \leq 0.25$, a dense, hot H+, and a dense colder He+

For $x_r > 0.25$, a dense, hot H+, tenuous He+



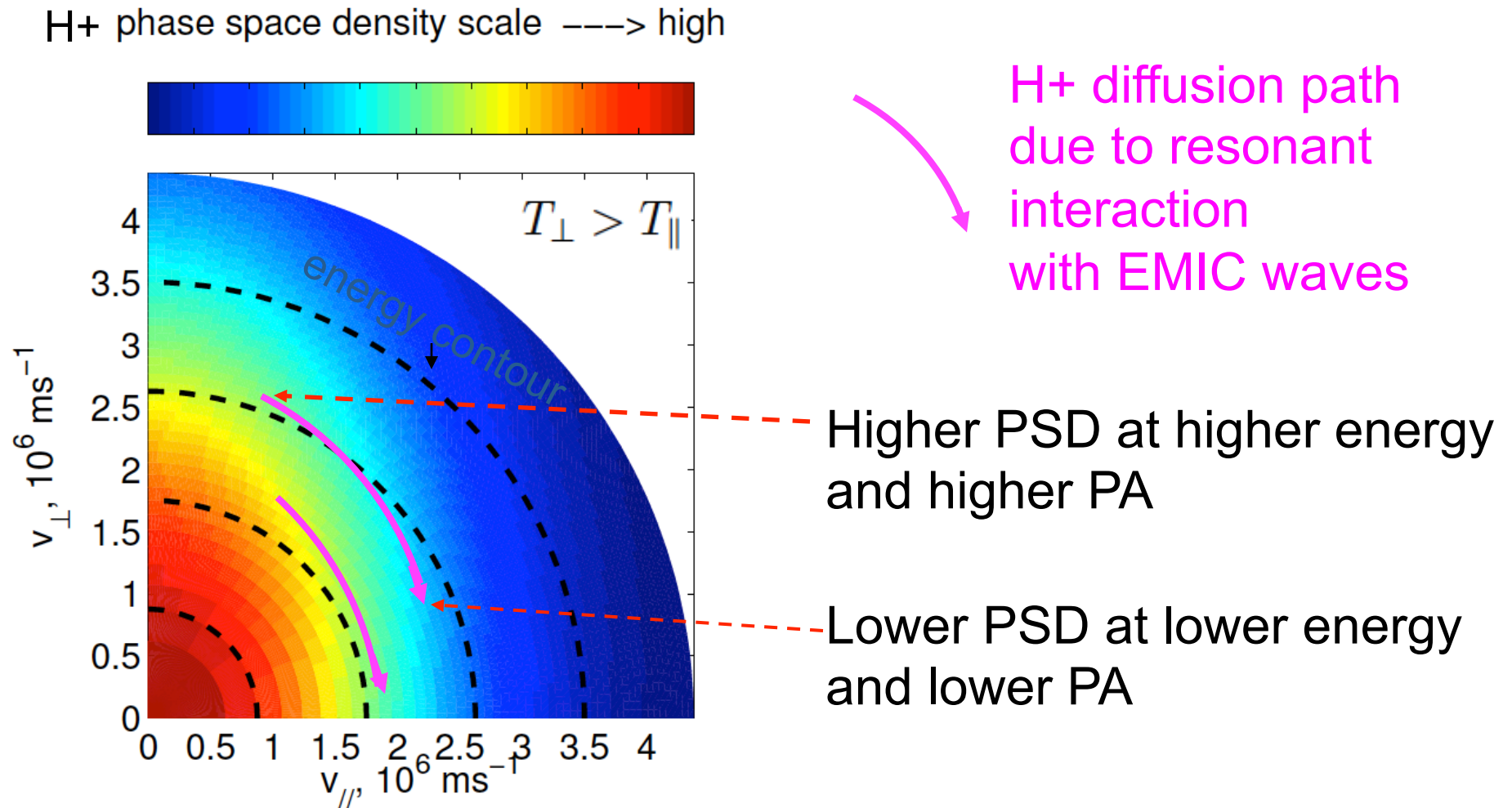
From RAM simulation
[Chen et al., 2010]

Within reasonable constraints $\eta_{hh} \leq 10\%$ and $A_{hh} \leq 2$, then a relatively extreme condition ($f > \sim 25$, $A_{hh} > 1$) is required to scatter MeV electrons.

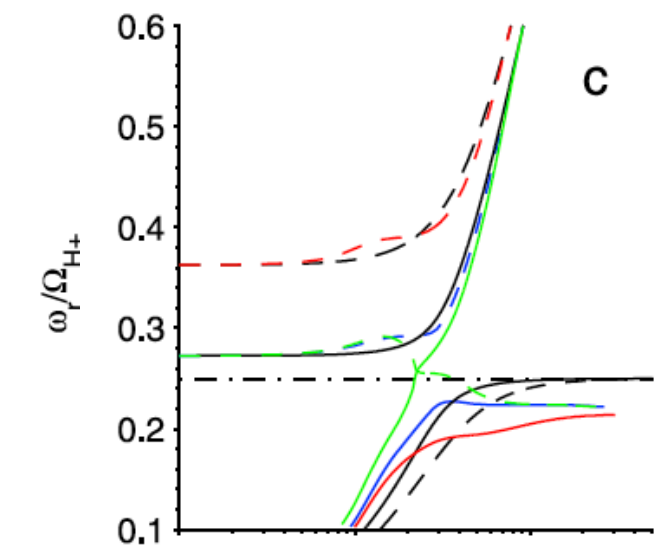
Summary

- Hot plasma effects due to H⁺ and He⁺ produce a significant modification in the cold plasma description of EMIC waves, especially near Ω_{He^+}
- The modification is important when evaluating relativistic electron scattering rate.
- Instability of EMIC waves at Ω_{He^+} is due to the dominance of hot RC H⁺ over warm He⁺, and provides an efficient mechanism for heating He⁺.
- Extreme condition is required to excite waves capable of resonating MeV electrons.

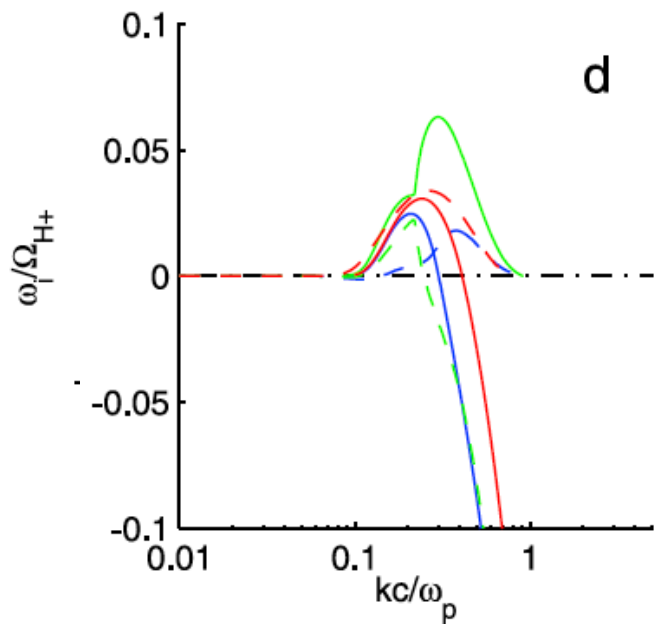
Generation mechanism of EMIC waves

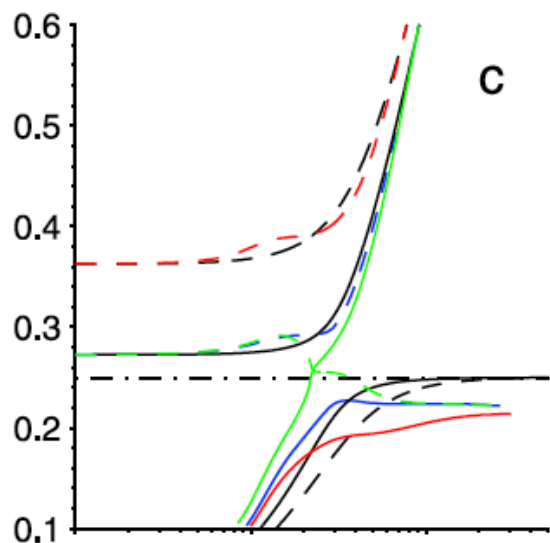


Ring current H+ population with temperature anisotropy $T_{\perp} > T_{\parallel}$ is unstable for **EMIC waves near field-aligned propagation ($k \parallel B$)** [Kennel and Petschek 1966].

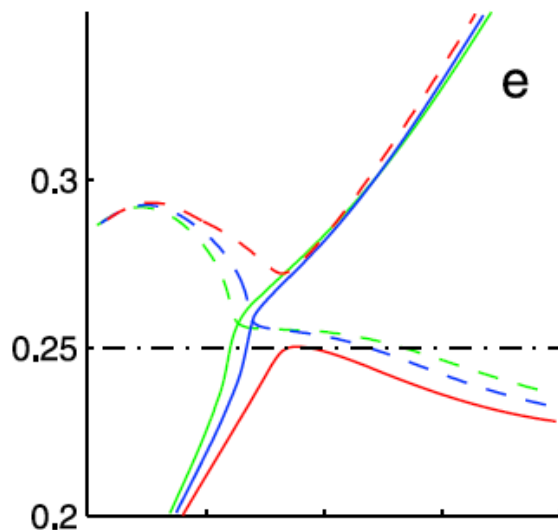


$\eta_{he}=3\%$, $\eta_{hh}=5\%$
 $\eta_{he}=3\%$, $\eta_{hh}=10\%$
 $\eta_{he}=15\%$, $\eta_{hh}=10\%$

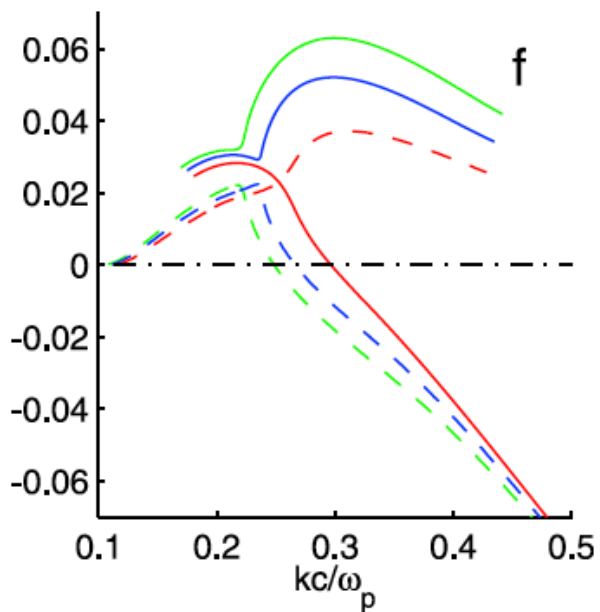
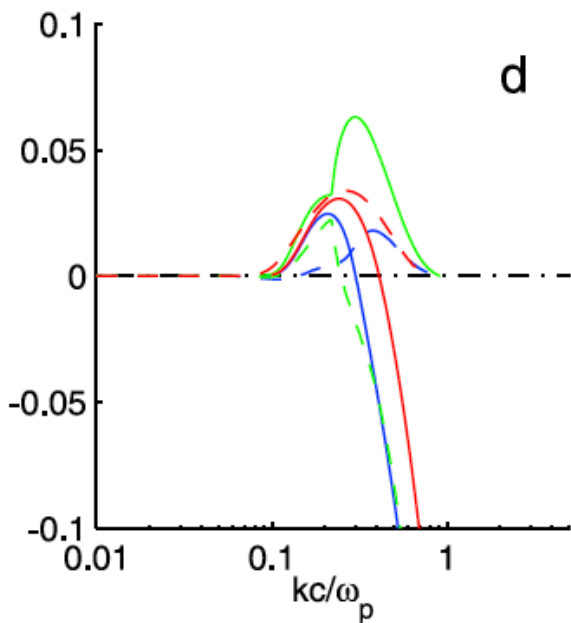


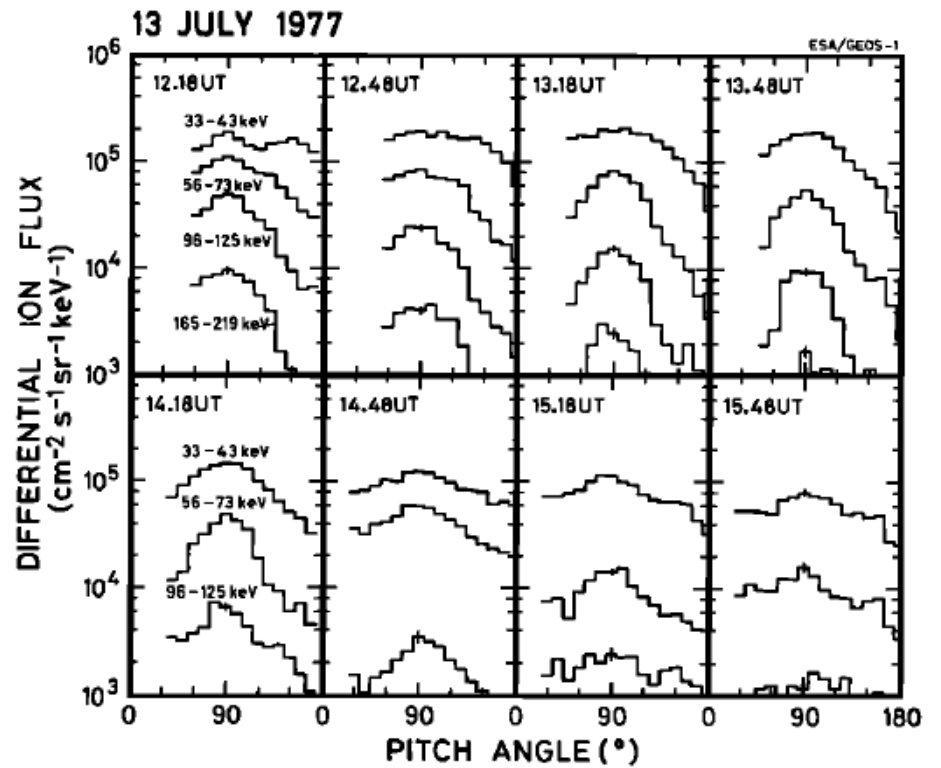
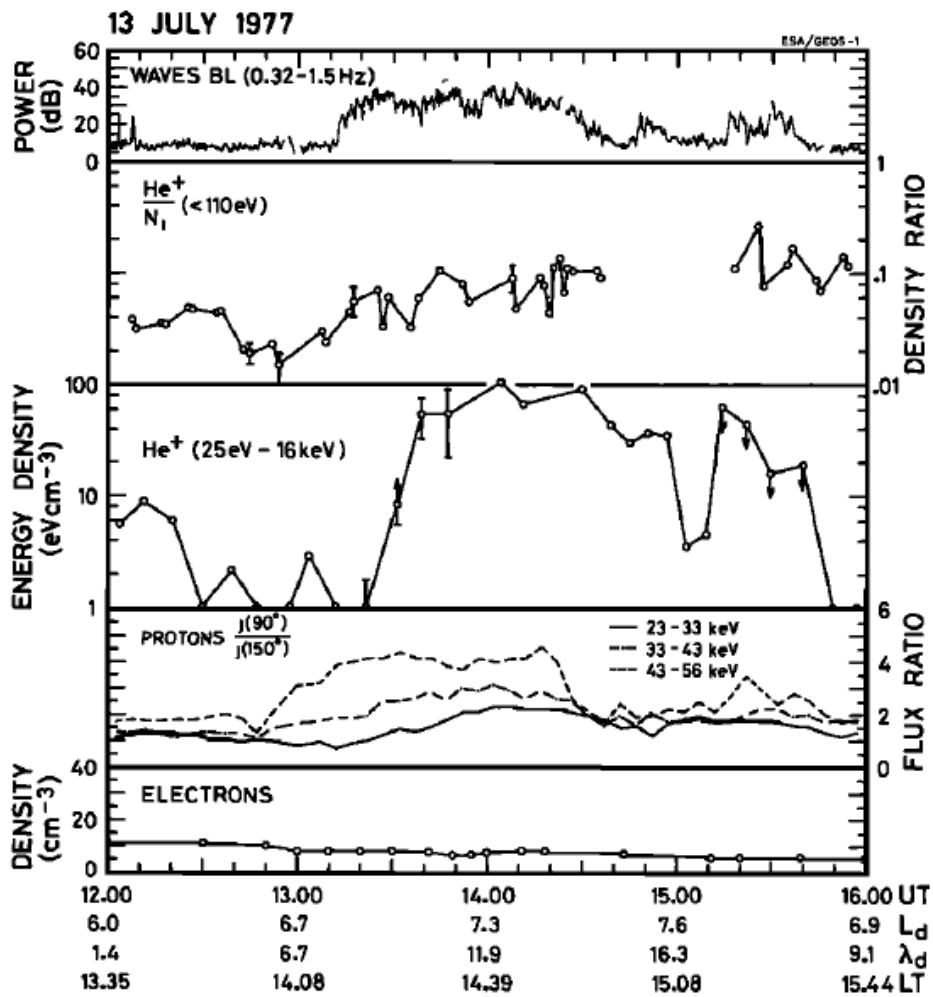


$\eta_{he}=3\%, \eta_{hh}=5\%$
 $\eta_{he}=3\%, \eta_{hh}=10\%$
 $\eta_{he}=15\%, \eta_{hh}=10\%$



$\theta=10^\circ$
 $\theta=0^\circ$
 $\theta=15^\circ$





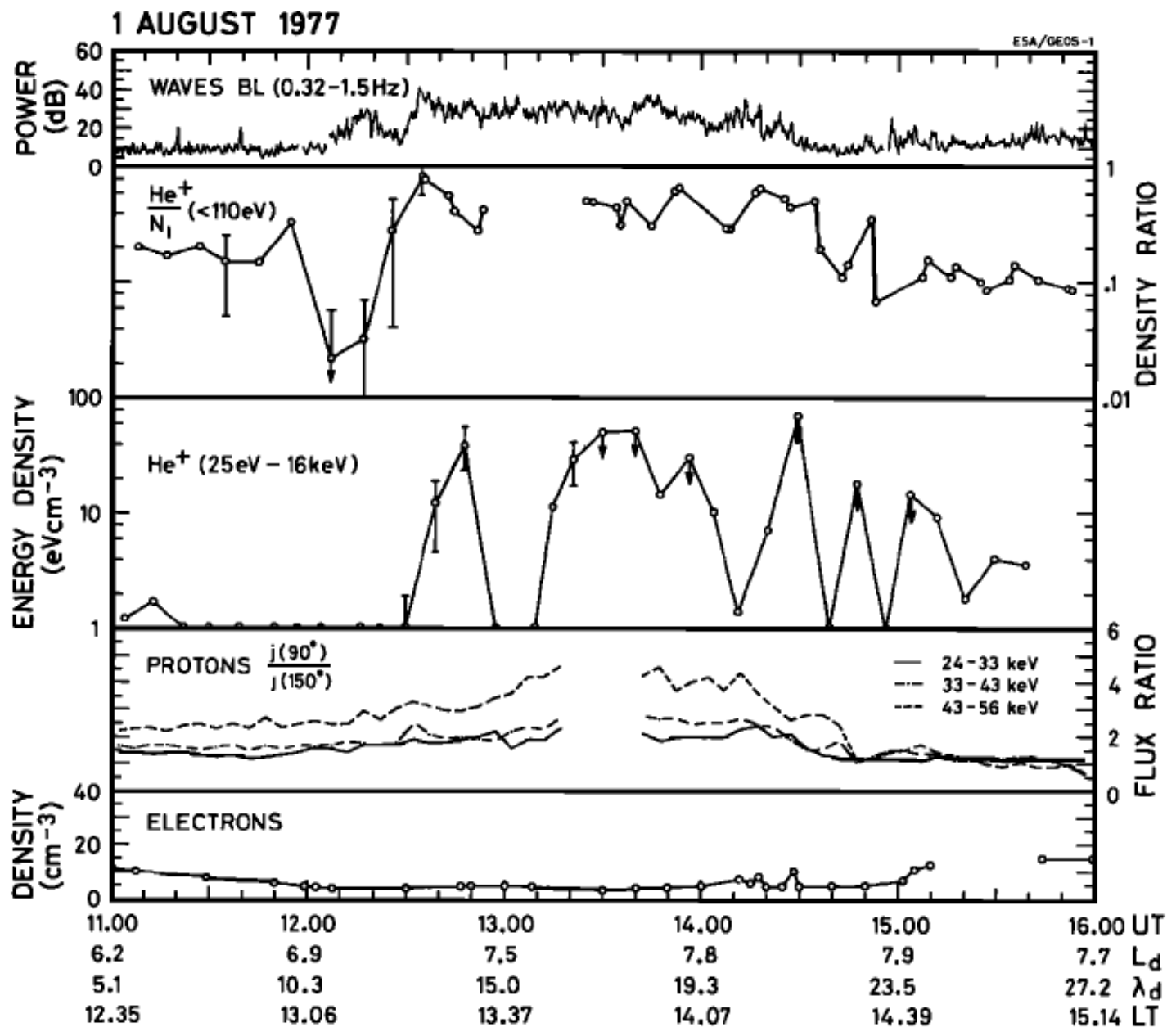


Fig. 11. Composite data for August 1, 1977 (see caption for Figure 9).

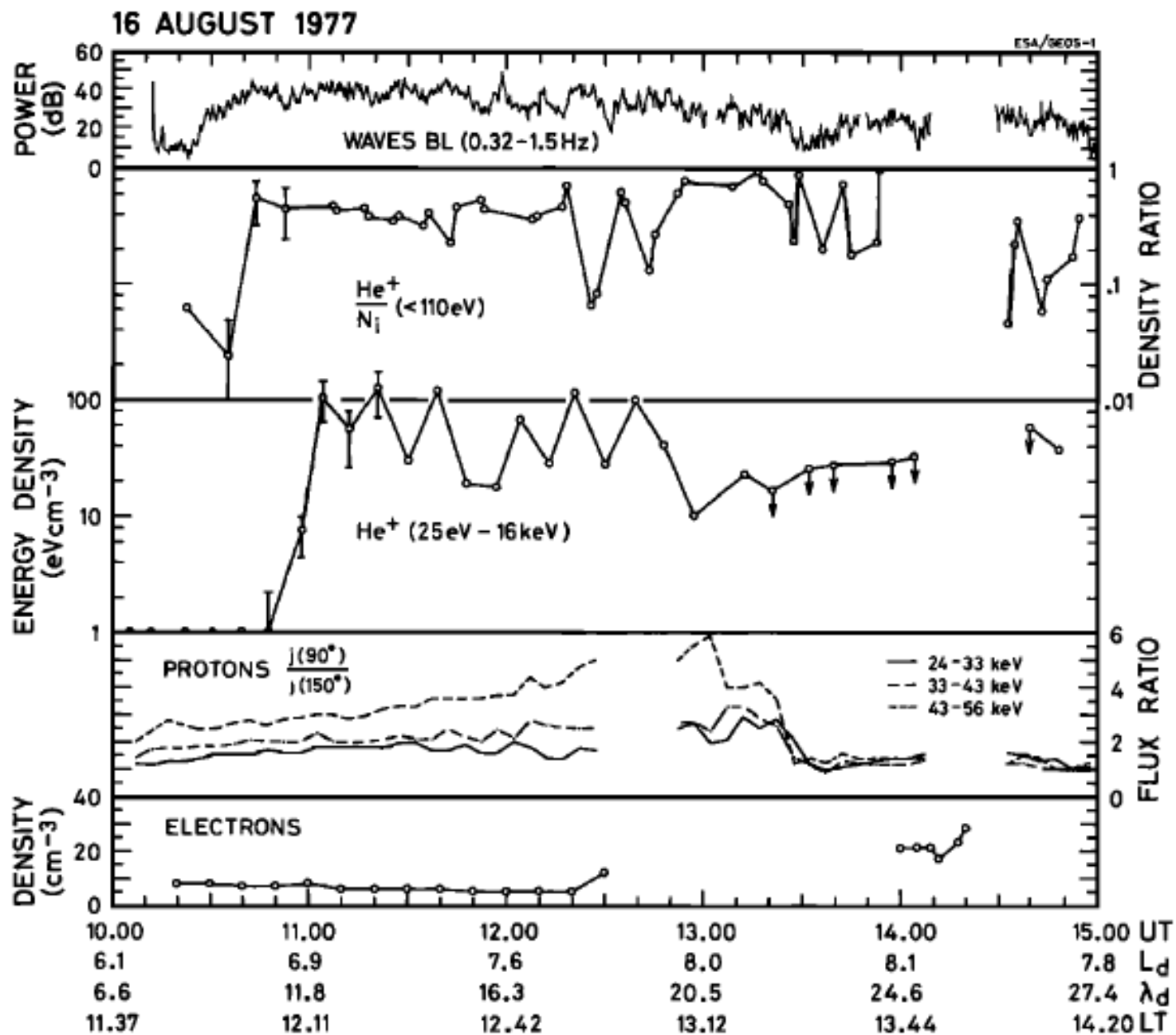


Fig. 12. Composite data for August 16, 1977 (see caption for Figure 9).

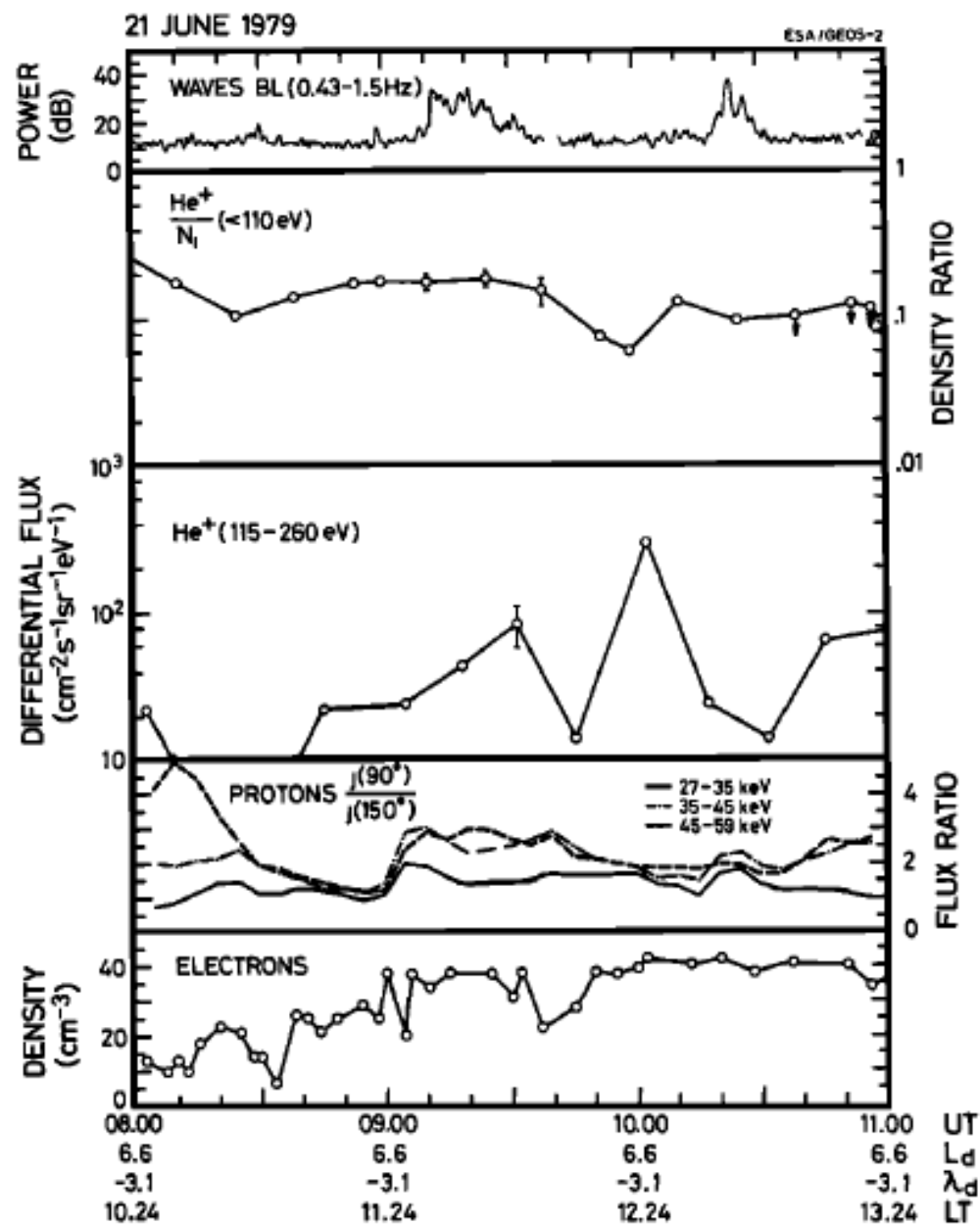


Fig. 13. Composite data for June 21, 1979 (see caption for Figure 9). Note that in the middle panel the differential He⁺ flux at 115-260 eV has been plotted instead of the He⁺ energy density (see text).

TABLE 3. Acceleration of He⁺ Ions by ICWs

	(1) Coincident Strong He ⁺ Fluxes	(2) Coincident Weak He ⁺ Fluxes	(3) No Su- prathermal He ⁺ Detected
Waves present	17 (31%)	20 (37%)	15 (28%)
No waves present		2 (4%)	