Horizontal Convective Rolls

Asai papers & Simulations w/ ARPS

Asai (1970a)

- Effect of vertical shear on roll orientation
- Boussinesq derivation equations similar to shear instability derivation
 - Negative Richardson numbers (reported as positive numbers) represent unstable environments
 - Presumed solutions similar to before, but solved numerically
- Figure 2
 - Most unstable mode is stationary relative to flow and becomes smaller in size as -Ri increases



Fig. 2. Amplification rate of perturbation as a function of the Richardson number R_i (ordinate) and the wavenumber k^* (abscissa). Solid lines are isopleths of amplification rate (in units of 10), dash-dotted line indicates the maximum amplification rate, and dotted line separates the stationary unstable perturbation from the transitive one.

Asai (1970a) Fig. 2

• -Ri vs. k (thermal instability increases upward; wavelength increases to left)

- Left of dotted curve represents waves (rolls) stationary with respect to flow; propagating rolls to right
- Wavelength of **most unstable mode** (fastest growing solution that will dominate) becomes smaller as environment becomes more unstable [dashed curve]

• Most unstable solution is stationary with respect to flow for all unstable environmental conditions



Fig. 8. Variations of vertical momentum transfer ⟨U*W*⟩[†] (solid line) and amplification rate of perturbation σ* (broken line) with the ratio between the wavenumbers in the x and y directions., ky/kx, for different values of R_i. The numeral labelled at each curve denotes the value of R_i. These are for the case of R_a=10⁴ and k*=2.

Asai (1970a) Fig. 8

- Consider roll wavelengths Lx and Ly. Rolls aligned along x-axis have Lx >> Ly.
- Consider vertical shear oriented along the x-axis
- Horizontal axis is $k_y/k_x = L_x/L_y$ representing *roll orientation*
- Large L_x/L_y means rolls parallel with the vertical shear vector (*longitudinal rolls*). Small L_x/L_y means rolls oriented perpendicular to shear (*transverse rolls*)
- Vertical axis (labeled at right) is amplification rate for various roll orientations

More...



Fig. 8. Variations of vertical momentum transfer $\langle U^*W^* \rangle^{\dagger}$ (solid line) and amplification rate of perturbation σ^* (broken line) with the ratio between the wavenumbers in the x and y directions., k_y/k_x , for different values of R_i . The numeral labelled at each curve denotes the value of R_i . These are for the case of $R_a = 10^4$ and $k^* = 2$.

Asai (1970a) Fig. 8 (continued)

• Amplification rate vs. roll orientation for various values of -Ri (thermal instability; <u>dashed curves</u>)

- <u>Shear-parallel</u> rolls always have largest growth rate
- For marginally unstable environments (-Ri = 0.5), shearperpendicular rolls are suppressed
- For very unstable environments (-Ri > 10) *all* orientations are unstable
- (Ignore solid curves)

Asai (1970a)

- Figure 8 summary
 - Shear-parallel (longitudinal) rolls always favored
 - Small instability shear-perpendicular (transverse) rolls have very small growth rates
 - Large instability all possible orientations grow quickly
 - Cells?

Asai (1972)

- Thermally unstable but -Ri not varied
- Directional and speed shear
- Case I shear vector still constant w/ z
 - Shear vector is NW-SE in example
 - Figure 2: growth rate max for Lx = Ly
 - Rolls still line up parallel to shear vector
- Case 2 shear vector turns with height
 - Figure 6: three maxima (two shown)
 - Parallel to shear in <u>upper</u> part of shear layer
 - Parallel to shear in lower part of shear layer
 - Perpendicular to shear (inflection point instability)

Asai (1972) sign convention



Wavelengths are Lx, Ly

Wavenumbers are Kx, Ky

Both can be negative depending on roll orientation

For NW-SE rolls Kx, Ky >0 and Lx, Ly > 0

Asai Case 1: Shear NW-SE (above)







Fig. 4. Schematic diagram showing characteristics of thermal convection rolls in relation to the basic flow. Dashed lines indicate the axis of the preferred roll convection and a broad arrow denotes the phase velocity of the roll convection.

Asai (1972) Case I

Asai (1972) Case I



Fig. 2. Amplification rates in units of 0.1 as a function of the wavenumbers, k_x and k_y , for Case (I) with $a_1=1$, $R_i=1$ and $R_a=10^4$. A dash-dotted line indicates a maximum amplification rate for a given wavenumber.

- Axes are E-W and N-S wavenumbers
- Contoured is amplification rate
- Shear oriented NW-SE
- Largest growth rate for rolls with Lx = Ly > 0; i.e., *aligned along shear vector*
- Growth rate max for <u>inter-</u> mediate wavelengths

Asai (1972) Case II



Shear vector varies w/ Height

Upper layer shear remains NW-SE

Asai (1972) Case II - v profile

Note V component has inflection point(s) [at z=.25 and .75] >>>

U component does not (not shown)



Asai (1972) Case II



Fig. 6. Same as in Fig. 2 but for Case (II) with $a_2=1$ and b=2.

More...

- Fig. 6 largest amplification rate again "nearly parallel" to shear vector (i.e., Kx = Ky) in upper part of layer (actually, they' re turned at some CCW angle to shear vector)
- Rolls "parallel" to shear vector in *lower* part of layer also appeared but are NOT shown (Ky < 0)
- Also a local max in amplification rate for rolls parallel to y-axis (Ky = 0) with long wavelengths (unexplained by Asai)

Asai (1972) Case II



Fig. 6. Same as in Fig. 2 but for Case (II) with $a_2=1$ and b=2.

 Another locally large amplification rate occurs for Kx = 0 (rolls parallel to x-axis, at angle to shear)

> That is inflection point instability which produces rolls oriented perpendicular to the wind component with the inflection point (here, the <u>v component</u>)

Asai (1970a) Case II



Fig. 7. Same as in Fig. 6 but $R_i = 10^{-2}$.

- Fig. 7 when <u>thermal</u> <u>instability removed</u>, only dynamical instability (inflection point instability) remains
- This proves the other local maxima were due to thermal instability

Revisit ARPS simulation



Vertical velocity at 1.5 km AGL (above the shear layer)





Vertical profiles of θ



What happens if the shear vector varies with height?

RUN03

RUN03 hodograph



Shear vector veers with height Little surface wind

Animation



Lack of rolls in RUN03...

- Not enough shear?
- Too much directional shear?
- Not enough wind near surface? (Needed for surface heat flux)

RUN11 same shear, added mean wind





RUN11 same shear, added mean wind



Smaller domain; same aspect ratio

What happens if we have <u>no</u> shear?

RUN06 - no (initial) shear



RUN06 - no (initial) shear



Shear created by surface friction

note small values

RUN07 no initial shear, <u>no drag</u>





Variation is very, very small



Cross-roll flow develops inflection point, but shear VERY small

- Monin-Obukhov length L
 - Ratio of vertical momentum flux to vertical heat flux (*negative* for strongly heated surface)
 - L magnitude large when heat flux small (i.e., early in day); decreases through afternoon
- Boundary layer depth z_i
- -z/L is large when PBL is very unstable
- Deardorff (1972): rolls exist for -z/L between 0 and 45
 - Other studies came up different ranges
 - Generally, with larger $-z_i/L$ rolls <u>less</u> likely
 - Therefore, rolls can change to cells as surface heats up



Early in day: no structure

Nolan Atkins



Surface heating increases; rolls appear

Nolan Atkins



Stronger heating; cells replace rolls

Nolan Atkins

Weckwerth's experiments



Roll behavior as function of surface heat flux Q_H

Plots at right show autocorrelation rather than vertical velocity

Small heat flux: rolls parallel to wind and wind shear

Rolls less coherent as surface heat flux increased; Turn CCW a bit first...

Weckwerth et al. (1997)

Weckwerth's experiments



Roll behavior as <u>surface</u> <u>wind speed</u> increased (fixed z_i)

Light surface winds -- rolls or cells?

Rolls more coherent as surface wind increased (shear has also increased)

Weckwerth et al. (1997)

Roll wavelength

• Kuettner (1971) observations/theory

$$L_x = 2\sqrt{2}z_i$$

 So as boundary layer depth z_i grows, horizontal roll spacing increases

Weckwerth's experiments





z_i 1.1 km

Varied PBL depth

1.6 km

Roll wavelength larger as PBL depth increases

2.0 km

Weckwerth et al. (1997)